

# On possible existence of pseudobinary mixed valence fluorides of Ag(I) / Ag(II): a DFT study

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**Abstract** The DFT calculations performed within local density approximation disclose conceivable existence of two novel mixed-valence Ag(I)/Ag(II) fluorides,  $\text{Ag}_2\text{F}_3$ , *i.e.*,  $\text{Ag(I)Ag(II)F}_3$  and  $\text{Ag}_3\text{F}_4$ , *i.e.*,  $\text{Ag(I)}_2\text{Ag(II)F}_4$ .  $\text{Ag}_2\text{F}_3$  is predicted to crystallize in three equally stable  $\text{NaCuF}_3$ -,  $\text{KAgF}_3$ -, or  $\text{CuTeO}_3$ -type structures, while  $\text{Ag}_3\text{F}_4$  should be isostructural to  $\text{Na}_2\text{CuF}_4$ . The calculated vibration-corrected energies of formation at 0 K of  $\text{Ag}_2\text{F}_3$  and  $\text{Ag}_3\text{F}_4$  (in their most stable polytypes) from binary fluorides are negative but small (respectively,  $-0.09$  eV and  $-0.21$  eV per formula unit). Formation of  $\text{Ag}_3\text{F}_5$  (which, in fact, is a mixed valence Ag(I)/Ag(III) salt) from binary fluorides is much less likely, since the energy of formation is quite positive of about a quarter eV. The predicted volumes per formula unit for all forms of  $\text{Ag}_2\text{F}_3$  are larger and that for  $\text{K}_2\text{CuF}_4$ -type  $\text{Ag}_3\text{F}_4$  is smaller than the sum of volumes of the corresponding binary fluorides;  $\text{Ag}_2\text{F}_3$  should not form at high pressure conditions due to a decomposition to the binary constituents.  $\text{Ag}_2\text{F}_3$  and  $\text{Ag}_3\text{F}_4$  should exhibit genuine mixed- and not intermediate-valence with quite different coordination spheres of Ag(I) and Ag(II). Nevertheless, they should not be electric insulators.  $\text{Ag}_2\text{F}_3$  is predicted to be a metallic ferrimagnet with a magnetic superexchange coupling constant,  $J$ , of  $-2$  meV while  $\text{Ag}_3\text{F}_4$

should be a metallic ferromagnet with  $J$  of  $+52$  meV. Since  $\text{Ag}_2\text{F}_3$  and  $\text{Ag}_3\text{F}_4$  are at the verge of thermodynamic stability, a handful of exothermic reactions have been proposed which could yield these as yet unknown compounds.

**Keywords** Band theory · Density functional theory · Fluorine · Mixed valence · Oxidizers · Phonons · Silver

## Introduction: why to search for mixed valence?

Mixed valence compounds constitute a fascinating and quite large family of solids synthesized in the laboratories but also occurring in nature, as exemplified by mineral magnetite  $\text{Fe(II)Fe(III)}_2\text{O}_4$  (archetypical magnet). The very existence of mixed valences within one solid phase is linked to the classical philosophical dilemma of ‘Buridan’s ass’ (Fig. 1): will the valences be mixed, indeed, *i.e.*, trapped at two crystallographically distinct sites (which cannot easily interconvert [1]) or rather will they exhibit an intermediate (*i.e.*, averaged) valence? In the late 1960s Robin and Day have presented a valuable classification of mixed-valence compounds [2] where a division to three distinct groups was proposed. The response to the ‘mixed-or-intermediate?’ question has been provided by simple but quantitative two-parabola models such as the one by Marcus [3], or the later substantially extended one [4]. Depending on the size of the model parameters (electronic mixing, vibronic mixing, force constant for bond stretching [5]) mixed valence compounds exhibit distinctly different electronic transport and magnetic properties as well as optical absorption spectra. Many of them, such as for example hole- or electron-doped copper oxides [6], show superconductivity.

Silver is no different from other transition metals and it may adopt mixed valence; the following compounds with

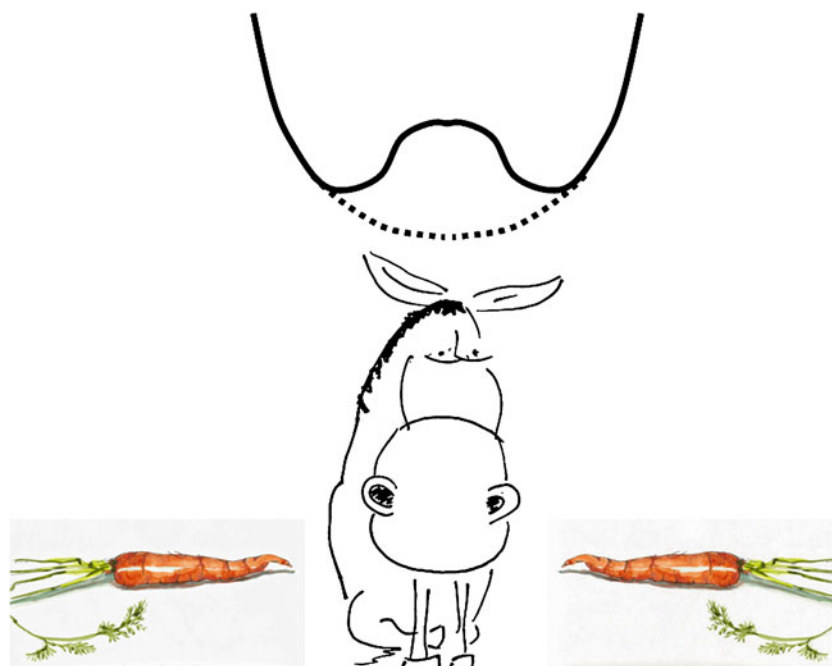
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This work is dedicated to eminent crystallographer and good friend, Michał Ksawery Cyrański, on his birthday

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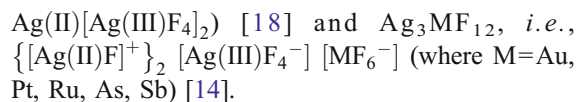


**Fig. 1** Illustration of the perpetual ‘Buridan’s ass’ dilemma of chemical compounds with an element at two different formal oxidation states: will they adopt a mixed valence (Robin & Day class I, localized, solid potential energy curve) or rather an intermediate one (Robin & Day class III, delocalized, dotted potential energy curve)? Mixed valence compound offer one more possibility: a fluctuating valence (Robin & Day class II). Buridan’s paradox’ of medieval logic

concerns the dilemma of an ass who is placed equidistantly from two piles of food of equal size and quality in a perfectly symmetrical situation. If the behavior of the ass is completely rational, it will have no reason to prefer one pile to the other and therefore cannot reach a decision over which pile to eat first, so it remains in its original position and starves

Ag at the two different oxidation states have been synthesized in the past (Table 1):

- (i) 0 and +1 for  $\text{Ag}_2\text{F}$  [7] and  $\text{Ag}_2\text{Ni(III)O}_2$  [8, 9];
- (ii) +1 and +2 for  $[\text{Ag(II)(tmc)(BF}_4)]_2[\text{Ag(I)}_6(\text{C}_2)(\text{CF}_3\text{CO}_2)_5(\text{H}_2\text{O})] \cdot \text{H}_2\text{O}$  (where tmc=1,4,8,11-tetramethyl-1,4,8,11-tetraazacyclotetradecane) [10], fluorosulfate  $\text{Ag(I)}_2\text{Ag(II)(SO}_3\text{F)}_4$  [11, 12],  $\text{Ag(I)}_2\text{Ag(II)(SbF}_6)_4$  [13],  $\text{Ag}_9\text{F}_{16}$ , *i.e.*,  $\text{Ag(I)}_2\text{Ag(II)}_7\text{F}_{16}$  has been mentioned but its synthesis was never confirmed (Bartlett N (2001) private correspondence)
- (iii) +1 and +3 for  $\beta\text{-AgF}_2$  [14],  $\text{Ag(I)Ag(III)O}_2$  [15] and  $\text{Ag(I)}_2(\text{Ag(III)}_5\text{O}_8)\text{L}$  where  $\text{L}=\text{NO}_3, \text{HF}_2$  etc. [16]
- (iv) +2 and +3 for  $\text{Ag}_3\text{O}_4$  [17],  $\text{Ag}_2\text{F}_5$  (*i.e.*  $\text{Ag(II)F[Ag(III)F}_4]$ ) [18, 19],  $\text{Ag}_3\text{F}_8$  (*i.e.*,



It is interesting to note that crystal environment of silver cations at two distinct formal oxidation states considerably differs for nearly all compounds listed above, which leads to a mixed- (class I) and not intermediate-valence, with metallic  $\text{Ag}_2\text{F}$  and  $\text{Ag}_2\text{NiO}_2$  as exclusive exceptions from this rule.

Fluorides of divalent silver are an intriguing class of compounds [20], since they show substantially covalent Ag–F bonding [21] despite a rather low oxidation state of the transition metal. Metallic conductivity has been suggested for salts exhibiting infinite  $[\text{AgF}^+]$  cations [22] as well as for related  $\text{KAgF}_3$  [23] and even superconductivity

**Table 1** The less known 20 mixed- or intermediate-valence compounds of silver at two various oxidation states, N

N	0	+1	+2	+3
0	X	$\text{Ag}_2\text{F, Ag}_2\text{NiO}_2$	not known	not known
+1	X	X	$[\text{Ag(tmc}^*)(\text{BF}_4)]_2[\text{Ag}_6(\text{C}_2)(\text{CF}_3\text{CO}_2)_5(\text{H}_2\text{O})] \cdot \text{H}_2\text{O}$ , $\text{Ag}_3(\text{SO}_3\text{F})_4$ , $\text{Ag}_3(\text{SbF}_6)_4$ , $\text{Ag}_9\text{F}_{16}$ (?)	$\beta\text{-AgF}_2$ , $\text{Ag}_2\text{O}_2$ , $\text{Ag(I)}_2(\text{Ag(III)}_5\text{O}_8)\text{L}$ ( $\text{L}=\text{NO}_3, \text{HF}_2, \text{BF}_4, \text{F}$ )
+2	X	X	X	$\text{Ag}_3\text{O}_4$ , $\text{Ag}_2\text{F}_5$ , $\text{Ag}_3\text{F}_8$ , $\text{Ag}_3\text{MF}_{12}$ ( $\text{M}=\text{Au, Pt, Ru, As, Sb}$ )

\* tmc=1,4,8,11-tetramethyl-1,4,8,11-tetraazacyclotetradecane

has been claimed [24] for the Be-Ag-F system with an unknown impurity (likely with O and H traces). Indeed, it has been claimed earlier that properly crystal-engineered fluorides of Ag(II) might exhibit superconductivity [20, 25, 26]. Mixed valence fluoroargentates(II) would thus constitute a valuable extension of the solid state chemistry of Ag(II) and Ag(I) cations, which should be analogous to electron-doped, *i.e.*, Cu(II)/Cu(I) oxide superconductors such as  $\text{Nd}_{2-x}\text{Ce}_x\text{CuO}_4$  [27]. They might also allow the formation of the first intermediate valence  $\text{Ag}^{n+}$  fluoride, where  $1 < n < 2$ . This formation could be spontaneous or via chemical doping or high-pressure metallization [28], with concomitant consequences for the electronic transport. At last but not least,  $\text{Ag}_3\text{F}_5$ ,  $\text{Ag}_2\text{F}_3$  and  $\text{Ag}_3\text{F}_4$  would enrich the spectrum of known fluorides of silver:  $\text{Ag}_2\text{F}$ ,  $\text{AgF}$ ,  $\text{AgF}_2$ ,  $\text{AgF}_3$ ,  $\text{Ag}_2\text{F}_5$ , and  $\text{Ag}_3\text{F}_8$ .

## Methodology

### Computational details

Results presented in this study are based on solid-state calculations done within the density functional theory (DFT) framework using the projector-augmented wave method (PAW) [29] as implemented in the Vienna *ab initio* simulation package (VASP, ver. 4.6 [30–32]). For the exchange-correlation part of the Hamiltonian, the local density approximation (LDA) with the Vosko-Wilk-Nusair exchange-correlation functional [33] has been applied. Full geometry optimization was performed with the SCF convergence criterion set to  $10^{-7}$  eV. The ionic relaxation was continued until the forces on individual atoms were less than  $1 \text{ meV } \text{Å}^{-1}$ . The spacing between the k-points for the k-point mesh generation was typically  $0.45 \text{ Å}^{-1}$  or denser. The valence electrons of highly electronegative fluorine as well as silver at high oxidation states were described by plane waves with a kinetic energy cutoff of 800 eV which provided excellent convergence of total energy of less than  $1 \text{ meV/atom}$ .

Compounds of Ag(II) with a  $4d^9$  electronic configuration are paramagnetic and they often show peculiar magnetism [34]. However, we have observed that allowing for spin polarization does not lead to remarkable modifications of structural features or the energy of polymorphs studied here (similarly to our earlier results for Ag(II)SO<sub>4</sub> and Ag(II)F<sub>2</sub> [35, 36]); this can be understood if one recalls that magnetic coupling usually constitutes a very small contribution to the electronic energy. This is especially true for compounds containing Ag(II) cation with its single unpaired valence electron; magnetic coupling is usually very weak for such systems and it comes with negligible effect on crystal structure as well as total energy (up to 0.05 eV per one paramagnetic center). As a consequence, results of all

structural optimizations come from non-spin-polarized LDA calculations.

The *electronic* structure was calculated using both the LSDA and LSDA+U methods with  $U(\text{Ag}_{4d})=U(\text{F}_{2p})=4 \text{ eV}$ , and  $J=1 \text{ eV}$  for both elements (parameters were taken from the previous theoretical study for fluoroargentates(II) [37]). The Dudarev's formalism for U was applied [38]. Magnetic cells were constructed for the following supercells: (1 x 1 x 1) for  $\alpha\text{-Ag}_2\text{F}_3$  ( $Z=4$ ), ( $\sqrt{2}x \sqrt{2}x1$ ) for  $\beta\text{-}$  and  $\gamma\text{-Ag}_2\text{F}_3$  and for  $\alpha\text{-Ag}_3\text{F}_4$  ( $Z=8$ ), (2 x 1 x 1) for  $\beta\text{-Ag}_3\text{F}_4$  ( $Z=4$ ), and later symmetrized to monoclinic (or triclinic, for  $\alpha\text{-Ag}_2\text{F}_3$ ) magnetic cells ( $Z=4$  for all polymorphs). The sign of the magnetic superexchange (antiferromagnetic or ferromagnetic, intra-sheet, intra-chain, inter-chain or inter-sheet) for  $\text{Ag}_2\text{F}_3$  was initially guessed from orbital criteria for the occurrence of magnetism and later confirmed by the calculations of the magnetic superexchange constant J through probing various spin ordering topologies. Due to the presence of low-spin Ag(III) and closed-shell Ag(I),  $\alpha\text{-Ag}_3\text{F}_5$  will be diamagnetic, and thus no spin-polarized calculations were done.

The resource- and time-demanding calculations of the full phonon dispersion were not performed; instead, phonon frequencies at the center of the first Brillouin zone ( $\Gamma$ ) were calculated using VASP. Numerical values for all extensive properties are given per formulae unit (FU) of each compound. Typically, the most stable structures are discussed in this work.

### Structural models considered

The energy landscape of a solid with a given stoichiometry may in principle be very complex, so a multitude of chemically reasonable minima should be probed if no experimental structural data is available. The strategy of obtaining the dynamically stable structures used here relies on chemical intuition as well as on selection of starting structures which have a reasonable chance to be isostructural to the studied one. It is important that structural leitmotifs observed for the fluorides of Ag(II) are very similar to those for Cu(II) fluorides, with many known examples of isostructural or structurally tightly-related compounds ( $\text{Cs}_2\text{AgF}_4$  [39],  $\text{Rb}_2\text{AgF}_4$  [40] and  $\alpha\text{-K}_2\text{AgF}_4$  [37] vs.  $\text{K}_2\text{CuF}_4$  [41],  $\beta\text{-K}_2\text{AgF}_4$  [42] vs.  $\text{Na}_2\text{CuF}_4$  [43],  $\text{KAgF}_3$  [37] vs.  $\text{KCuF}_3$  [44, 45] etc.). In consequence, we have tested the following structural models:

- (i) For  $\text{Ag}_2\text{F}_3$ : Pbnm  $\text{KAgF}_3$ -type [37], Pmcn  $\text{CuTeO}_3$ -type [46], P-1  $\text{NaCuF}_3$ - or  $\text{AgCuF}_3$ -type [47, 48], C222<sub>1</sub>  $\text{BaVS}_3$ -type [49]
- (ii) For  $\text{Ag}_3\text{F}_4$ :  $\text{P}2_1/c$   $\beta\text{-K}_2\text{AgF}_4$ - vel  $\text{Na}_2\text{CuF}_4$ -type [42, 43],  $\text{Cmca}$   $\alpha\text{-K}_2\text{AgF}_4$ -type [37], and  $\text{I}4\text{mmm}$   $\text{Nd}_2\text{CuO}_4$ -type [50]

(iii) For  $\text{Ag}_3\text{F}_5$ : for this rare stoichiometry, we have used P4mbm a defected- $\text{K}_2\text{RbPdF}_5$ -type with Rb atoms removed [51], Imma  $\text{CsPd}_2\text{F}_5$ -type [52],  $\text{P2}_1/\text{n}$   $\text{CsCu}_2\text{F}_5$ -type [53], and I4mmm disordered  $\alpha$ - $\text{CsSn}_2\text{F}_5$ -type with one kind of fluoride anions enforced into a special  $(\frac{1}{2} \frac{1}{2} 0)$  crystallographic position to obtain ordering on anionic sites (which is necessary to perform extended DFT calculations) [54].  $\text{Rb}_2\text{AgF}_5$  has been claimed but, regretfully, its crystal structure is not known [55].

The coordination sphere of silver was chemically meaningful for all polymorphs studied (*i.e.*, octahedral or square-planar for Ag(II), linear, octahedral, pseudo-cubic or even one with a larger coordination number for Ag(I)). To assure dynamic stability for each structural type studied, we were following vectors of these normal vibrational modes which exhibited imaginary frequencies in the calculated phonon spectra, until those imaginary modes have disappeared. This approach has been applied in the past to predict the as yet unknown fluorides  $\text{Au}(\text{I})\text{F}$  [56],  $\text{XeAuF}$  [57] etc.

Building structural models for various fluorides of silver one might consider disproportionation of 2 Ag(II) to Ag(I)+Ag(III). For example,  $\text{Ag}(\text{I})\text{Ag}(\text{II})\text{F}_3$  is equivalent to  $\text{Ag}(\text{I})_{1.5}\text{Ag}(\text{III})_{0.5}\text{F}_3 \equiv \text{Ag}(\text{I})_3\text{Ag}(\text{III})\text{F}_6$  while  $\text{Ag}_3\text{F}_5$  to  $[\text{Ag}(\text{I})_2\text{F}][\text{Ag}(\text{III})\text{F}_4]$  as far as stoichiometry is considered. Coexistence of Ag(I) and Ag(III) is seldom achieved [14] since Ag(III) (either low- or high-spin) is stabilized only in a very basic environment, as for example in  $\text{KAgF}_4$  [58] or  $\text{Cs}_2\text{KAgF}_6$  elpasolite [55]. Our previous calculations for  $\text{Ag}(\text{I})\text{Ag}(\text{III})\text{F}_4$ , (*i.e.*, a disproportionated  $\beta$  form of  $\text{Ag}(\text{II})\text{F}_2$ ) [36] have shown that disproportionation of Ag(II) in a fluoride environment is slightly thermodynamically disfavored, in contrast to simple oxides (for example,  $\text{Ag}(\text{I})\text{Ag}(\text{III})\text{O}_2$  is a stable disproportionated form of a hypothetical  $\text{Ag}(\text{II})\text{O}$  [59]). As will be shown in the next section, the lowest energy polymorph of  $\text{Ag}_3\text{F}_5$  has a formulation as  $[\text{Ag}(\text{I})_2\text{F}][\text{Ag}(\text{III})\text{F}_4]$ .

### The lowest energy polymorphs of $\text{Ag}_3\text{F}_5$ , $\text{Ag}_2\text{F}_3$ and $\text{Ag}_3\text{F}_4$

#### Crystal structures

Let us first discuss aspects of crystal structures, topology and chemical bonding of the lowest energy polymorphs of three hypothetical fluorides of silver; the data regarding the predicted unit cells are contained in Tables 2 and 3.

The lowest energy polymorph of  $\text{Ag}_3\text{F}_5$  (from now on as  $\alpha$  form) found is tetragonal, of the defected- $\text{K}_2\text{RbPdF}_5$ -type (P4/mbm, Fig. 2A). Its crystal structure is composed of the

**Table 2** The calculated lattice parameters for a few intermediate-valence compounds of silver. Lattice constants for  $\beta$ - and  $\gamma$ - $\text{Ag}_2\text{F}_3$  are listed for standard Pnma settings

Compound	a /Å	b /Å	c /Å	$\alpha$ /°	$\beta$ /°	$\gamma$ /°
$\alpha$ - $\text{Ag}_3\text{F}_5^*$	6.089	6.089	6.272	90	90	90
$\alpha$ - $\text{Ag}_2\text{F}_3$	5.397	5.882	8.569	90.05	90.96	89.99
$\beta$ - $\text{Ag}_2\text{F}_3$	5.881	8.418	5.506	90	90	90
$\gamma$ - $\text{Ag}_2\text{F}_3$	6.171	8.071	5.291	90	90	90
$\alpha$ - $\text{Ag}_3\text{F}_4$	5.526	10.651	6.466	90	90	90
$\beta$ - $\text{Ag}_3\text{F}_4$	3.514	9.179	5.708	90	90.01	90

alternating  $[\text{Ag}_2\text{F}]_2$  and  $[\text{AgF}_4]$  layers. Coordination of  $[\text{AgF}_4]$  units is square planar with four identical Ag–F bonds at 1.999 Å; the very short bond lengths, atypical for Ag(II), suggest the presence of Ag(III). The planes of the neighboring  $[\text{Ag}(\text{III})\text{F}_4^-]$  anions are perpendicular to one another. Ag(I) is coordinated by eight fluoride anions (CN=8) with two 2.249 Å, two 2.268 Å and four 2.570 Å separations.  $\text{Ag}_3\text{F}_5$  thus resembles structurally to some extent  $\text{Ag}(\text{I})\text{Ag}(\text{III})\text{F}_4$  (*i.e.*, a disproportionated  $\beta$  form of  $\text{Ag}(\text{II})\text{F}_2$ ) [14, 36].

Three nearly energy-equivalent polymorphs of  $\text{AgAgF}_3$  of similar topology have been found during theoretical scrutiny. The first one, triclinic (P-1), hereafter referred to as  $\alpha$ -**AgAgF<sub>3</sub>** ( $\text{NaCuF}_3$ -type, Fig. 2B) is a distorted perovskite type, pseudo-orthorhombic and closely related to orthorhombic  $\beta$ -**AgAgF<sub>3</sub>** (see below). There are two non-equivalent Ag(II) centers in the structure. Both Ag(II) cations adopt a 2+2+2 coordination which resembles an elongated octahedron (I: 2x2.141 Å, 2x2.162 Å, 2x2.461 Å, *i.e.*, 2.255 Å on average; II: 2x2.084 Å, 2x2.106 Å, 2x2.535 Å, *i.e.* 2.242 Å on average). The first coordination sphere of Ag(I) is in the form of a distorted trigonal bipyramid (CN=6, bond lengths 2.211 Å, 2.230 Å, 2.248 Å, 2.404 Å, 2.485 Å, 2.529 Å, with average distance of 2.351 Å) as far as all separations below 2.60 Å are considered. The  $[\text{Ag}(\text{II})\text{F}_6]$  octahedra share the corners; the puckered  $[\text{AgF}_2]$  sheets separated by  $[\text{AgF}]$  layers may be distinguished in the crystal structure of this compound. Half of the  $[\text{AgF}_6]$  octahedra are elongated in the direction more-less perpendicular and another half in the direction parallel to the  $[\text{AgF}_2]$  sheets, rendering  $\alpha$ -**AgAgF<sub>3</sub>** a unique structure.

$\beta$ -**AgAgF<sub>3</sub>** is closely related to the  $\alpha$  form. It is a classic case of the orthorhombically distorted ABF<sub>3</sub> perovskite where too small size of the 12-coordinated B cation leads to the tilting of the  $[\text{AF}_6]$  octahedra [60] (Fig. 2C).  $\beta$ -**AgAgF<sub>3</sub>** adopts a Pbnm cell ( $\text{KAgF}_3$ -type) with a 2+2+2 coordination of Ag(II) which is not far from an elongated octahedron (2x2.143 Å, 2x2.194 Å, 2x2.477 Å). The first coordination sphere of Ag(I) is in the form of a distorted



**Table 3** The formation energies,  $\Delta E_f$ , for five different mixed valence fluorides of silver as calculated using the LDA method. The truncated (to  $\Gamma$ ) zero point energy corrections,  $\Delta ZPE_f(\Gamma)$ , and the resulting ZPE-corrected formation energies, are also given. ND=not determined

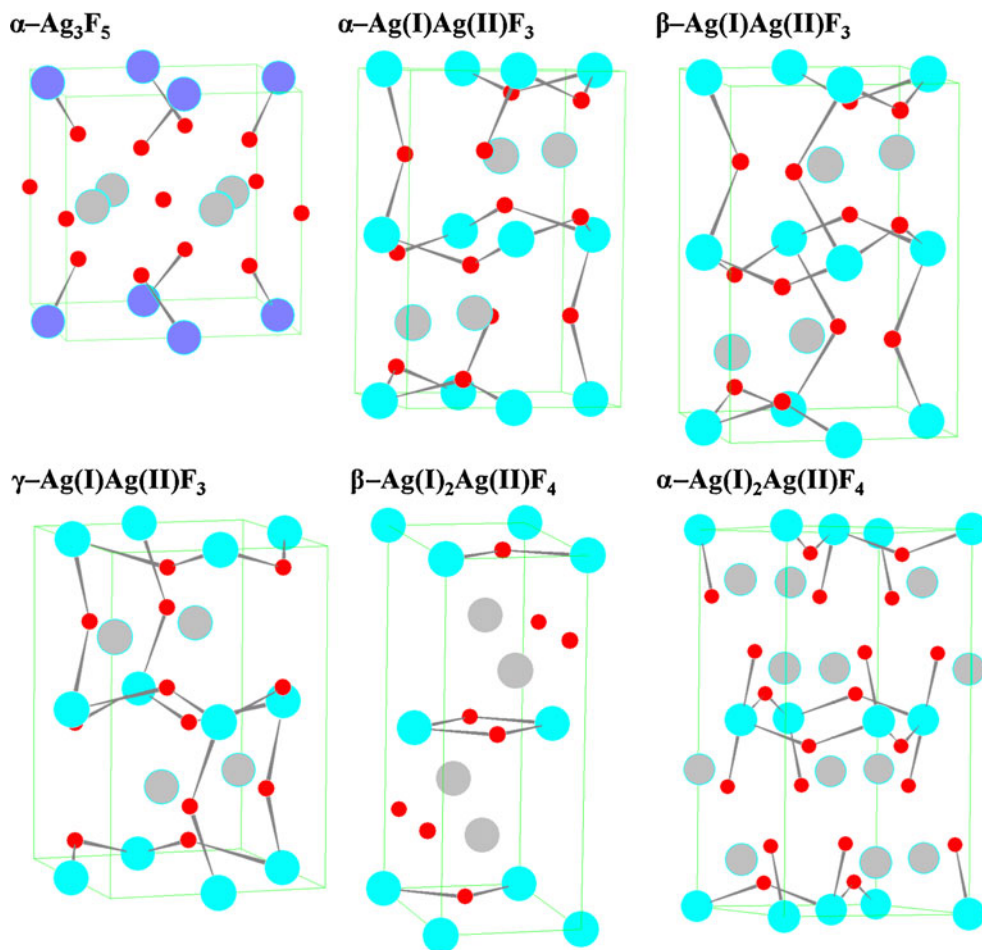
Compound	$\alpha$ -Ag <sub>3</sub> F <sub>5</sub>	$\alpha$ -Ag <sub>2</sub> F <sub>3</sub>	$\beta$ -Ag <sub>2</sub> F <sub>3</sub>	$\gamma$ -Ag <sub>2</sub> F <sub>3</sub>	$\beta$ -Ag <sub>3</sub> F <sub>4</sub>	$\alpha$ -Ag <sub>3</sub> F <sub>4</sub>
$\Delta E_f$ /eV	+0.27	-0.07	-0.04	-0.03	-0.17	+0.11
$\Delta ZPE_f(\Gamma)$ /eV	ND	-0.015	-0.033	-0.007	-0.038	-0.029
$\Delta E_f + \Delta ZPE_f(\Gamma)$ /eV	ND	-0.09	-0.07	-0.04	-0.21	+0.08

trigonal bipyramide (CN=6, bond lengths 2.152 Å, 2.161 Å, 2x2.352 Å, and 2x2.418 Å with average distance of 2.309 Å). The [Ag(II)F<sub>6</sub>] octahedra share the corners yielding the puckered [AgF<sub>2</sub>] sheets. It is also very interesting that – in contrast to KAgF<sub>3</sub> [37] – the [AgF<sub>6</sub>] octahedra are elongated in the direction perpendicular and not parallel to the sheets, thus rendering  $\beta$ -AgAgF<sub>3</sub> topologically more similar to the binary AgF<sub>2</sub> and not to ternary KAgF<sub>3</sub> [61, 62]. This feature comes from much smaller Lewis basicity of AgF as compared to KF, and has a strong impact on magnetism (see [Mixed valence, electronic structure, band gap at the Fermi level and magnetism](#)).

$\gamma$ -AgAgF<sub>3</sub> (CuTeO<sub>3</sub>-type), orthorhombic and layered like the  $\alpha$  and  $\beta$  phases, contains elongated [Ag(II)F<sub>6</sub>]

octahedra (2.081 Å, 2.143 Å, 2.390 Å) (Fig. 2D). However, the corner-sharing octahedra are now arranged in such a fashion that the Ag(II)–F–Ag(II) bridge is asymmetric, and the long axes of the octahedra are more-or-less within the propagation direction of the [AgF<sub>2</sub>] sheets (as seen also for Cs<sub>2</sub>AgF<sub>4</sub> or for KAgF<sub>3</sub>). Coordination sphere of Ag(I) cation resembles a distorted trigonal bipyramide (CN=6) with Ag(I)–F separations of 2x2.254 Å, 2.316 Å, 2.488 Å, and 2x2.639 Å (average distance is 2.432 Å). In this polymorph the Ag(II)–F bonds (2.205 Å on average) are shorter and stronger than for the  $\alpha$  (2.242–2.255 Å) and  $\beta$  (2.271 Å) phases. Simultaneously the Ag(I)–F bonds are weaker and longer (2.432 Å on average vs. 2.351 Å and 2.309 Å for  $\alpha$  and  $\beta$  phases, respectively).

**Fig. 2** Illustration of the crystal structures of the most stable polymorphs of Ag<sub>3</sub>F<sub>5</sub>, Ag<sub>2</sub>F<sub>3</sub>, and Ag<sub>3</sub>F<sub>4</sub>. Ag(I) – gray, Ag(II) – blue, Ag(III) – violet, F – red balls



Puckering of the  $[\text{AgF}_2]$  sheets – as measured by the Ag–F–Ag intra-sheet angles for  $\alpha$ ,  $\beta$ , and  $\gamma$  forms of  $\text{Ag}_2\text{F}_3$  ( $122.6^\circ$  and  $140.1^\circ$ ,  $136.5^\circ$  and  $130.7^\circ$ , respectively) – is in between those calculated for  $\text{AgF}_2$  ( $117.1^\circ$ ) and  $\text{KAgF}_3$  ( $157.3^\circ$ ) (note, the angle of  $180^\circ$  corresponds to flat  $[\text{AgF}_2]$  sheets). This is consistent with smaller cubic ionic radius of Ag(I) ( $1.42 \text{ \AA}$ ) as compared to K(I) ( $1.65 \text{ \AA}$ ).

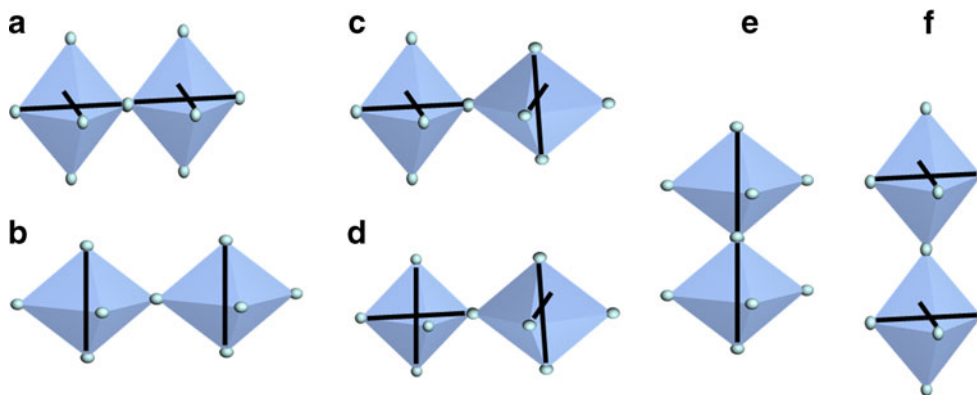
The most stable form of  $\text{Ag}_3\text{F}_4$  detected in this work (hereafter referred to as  $\beta\text{-Ag}_2\text{AgF}_4$ ) is monoclinic ( $\text{P}2_1/\text{c}$ ), and analogous to  $\beta\text{-K}_2\text{AgF}_4$  and  $\text{Na}_2\text{CuF}_4$  [42, 43, 63]. This polymorph (Fig. 2E) is characterized by the presence of infinite 1D  $[\text{AgF}_{4/2}]$  chains propagating along the  $a$  crystallographic direction. Coordination of Ag(II) is close to square planar ( $2 \times 2.193 \text{ \AA}$ ,  $2 \times 2.194 \text{ \AA}$ ,  $\angle \text{F-Ag-F} = 73.6^\circ$ ) ( $[\text{Ag(II)F}_4]$  rectangles share the edges) and thus different from the elongated octahedral one seen for  $\beta\text{-K}_2\text{AgF}_4$  [42]. Another important difference between both compounds is that for  $\beta\text{-K}_2\text{AgF}_4$  the  $[\text{AgF}_4]$  plaquettes are perpendicular while for  $\beta\text{-Ag}_2\text{AgF}_4$  they are parallel to the propagation direction of the infinite 1D chains. As we will see, this has important consequences for magnetism (*cf.* Mixed valence, electronic structure, band gap at the Fermi level and magnetism). Ag(I) cations are coordinated by six fluoride ligands (CN=6, bond lengths  $4 \times 2.307 \text{ \AA}$ ,  $2 \times 2.405 \text{ \AA}$  with an average distance of  $2.340 \text{ \AA}$ ).

Finally, the layered polymorph of  $\text{Ag}_3\text{F}_4$  considered in this work ( $\alpha\text{-Ag}_2\text{AgF}_4$ ) is orthorhombic ( $\text{Cmca}$ ), and analogous to  $\alpha\text{-K}_2\text{AgF}_4$  [37] (Fig. 2F). As expected, this polytype is much less stable from the infinite-chain  $\beta$ -form, due to spatial mismatch of the  $[\text{AgF}_2]$  and  $[\text{AgF}]$  sublattices. Coordination of Ag(II) is in the form of a compressed octahedron ( $2 \times 2.131 \text{ \AA}$ ,  $4 \times 2.243 \text{ \AA}$ , on average  $2.206 \text{ \AA}$ ) just like for  $\alpha\text{-K}_2\text{AgF}_4$  [37]. The first coordination sphere of Ag(I) forms a severely distorted tetrahedron (CN=4, bond lengths  $2.180 \text{ \AA}$ ,  $2.279 \text{ \AA}$ ,  $2 \times 2.327 \text{ \AA}$ , with average distance

of  $2.278 \text{ \AA}$ ). The  $[\text{Ag(II)F}_6]$  octahedra share the corners while forming the puckered  $[\text{AgF}_2]$  sheets separated by a spacer of two  $[\text{AgF}]$  layers. Puckering of the  $[\text{AgF}_2]$  sheets – as measured by the Ag–F–Ag intra-sheet angle of  $142.8^\circ$  – is intermediate between those calculated for  $\text{AgF}_2$  ( $117.1^\circ$ ) and  $\alpha\text{-K}_2\text{AgF}_4$  ( $168.0^\circ$ ). Again, this is consistent with smaller cubic ionic radius of Ag(I) as compared to K(I).

### Collective Jahn–Teller isomerism

It is intriguing that the three polymorphs of  $\text{Ag}_2\text{F}_3$  described in the preceding section have virtually identical energy (see Phonons at  $\Gamma$ : indicator of dynamic stability) which may suggest that their crystal topologies (and thus the fashions of how the elongated or compressed  $[\text{AgF}_6]$  octahedra are interconnected), are equally conceivable. There are three distinct cases (Fig. 3): (a)  $\beta\text{-Ag}_2\text{F}_3$  with a short bond–short bond pattern of intra-sheet AgF bonds within the puckered  $[\text{AgF}_2]$  layers and long inter-sheet AgF bonds, (b)  $\gamma\text{-Ag}_2\text{F}_3$  with bond length alternation (short–long) within the puckered  $[\text{AgF}_2]$  layers and short inter-sheet AgF bonds, and (c)  $\alpha\text{-Ag}_2\text{F}_3$ , an intermediate case between the two with partial bond length alternation within the puckered  $[\text{AgF}_2]$  layers (*i.e.*, half bonds alternate short–long and another half shows a short–short pattern), and concomitant partial elongation of the inter-sheet AgF bonds (half is long, half is short). Case (a) is analogous to situation incurred for  $\text{AgF}_2$ , case (b) to  $\text{KAgF}_3$ , while case (c) is unique and has not yet been observed for fluoroargentates(II). The described bond length patterns within  $[\text{AgF}_2]$  sheets are reflected in the lattice parameters:  $b_\beta (8.42 \text{ \AA}) \sim c_\alpha (8.57 \text{ \AA}) > b_\gamma (8.07 \text{ \AA})$  while  $\sqrt{(a_\beta^2 + c_\beta^2)} (6.75 \text{ \AA}) \ll \sqrt{(a_\alpha^2 + b_\alpha^2)} (7.98 \text{ \AA}) < \sqrt{(a_\gamma^2 + c_\gamma^2)} (8.13 \text{ \AA})$ , and in volumes  $V_\beta (272.6 \text{ \AA}^3) > V_\alpha (272.0 \text{ \AA}^3) > V_\gamma (263.5 \text{ \AA}^3)$ . The uniaxial stress in the direction perpen-



**Fig. 3** Illustration of several cases of the collective Jahn–Teller isomerism in fluoroargentates(II). Puckering of the  $[\text{AgF}_2]$  sheets (due to tilting of the octahedral) was omitted to simplify the picture; short Ag–F bonds are marked in black lines. Cases (B) and (E) involve compressed octahedra, the remaining cases the elongated ones, and

they are exemplified by: (a)  $\text{AgF}_2$ ,  $\beta\text{-Ag}_2\text{F}_3$ , (b)  $\alpha\text{-K}_2\text{AgF}_4$ ,  $\alpha\text{-Ag}_3\text{F}_4$ , (c)  $\alpha\text{-Ag}_2\text{F}_3$ , (d)  $\text{KAgF}_3$ ,  $\gamma\text{-Ag}_2\text{F}_3$ , and (e)  $\text{AgFBB}_4$ . To our knowledge, so far case (f) has not been observed or predicted for any compound of Ag(II)

dicular to the  $[\text{AgF}_2]$  sheets might thus result in the progressive  $\beta \rightarrow \alpha \rightarrow \gamma$  interconversions.

This phenomenon which may be labeled as a “collective Jahn–Teller isomerism”, testifies substantial plasticity of the coordination sphere of Ag(II) [64] but it has not yet been observed in experiment for any other fluoroargentate(II) or fluorocuprate (II). It was, however, theoretically anticipated for  $\text{K}_2\text{CuF}_4$  [65] and for odd-electron Li–Be alloy [66] at elevated pressure.

It is interesting that none of the polymorphs of  $\text{Ag}_2\text{F}_3$  studied here has a topology related to that of  $\alpha\text{-K}_2\text{AgF}_4$ , with a long bond–long bond pattern within a puckered  $[\text{AgF}_2]$  sheet (Fig. 3) and short apical AgF distances.

Impact of external pressure on formation and decomposition of mixed–valence fluorides of silver

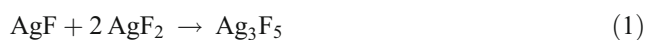
All mixed valence fluorides studied here have their volumes per FU larger from the sum of volumes of the corresponding binary fluorides. For example, the most stable form of  $\text{Ag}_3\text{F}_5$  has a volume that is  $10.5 \text{ \AA}^3$  (*i.e.*, 9.9 %) larger than the sum of the volumes of 2 AgF and 1  $\text{AgF}_2$ . Similarly, the most stable polymorphs of  $\text{Ag}_2\text{F}_3$  (NaCuF<sub>3</sub>-type, KAgF<sub>3</sub>-type and CuTeO<sub>3</sub>-type) have the respective differential volumes of  $+1.28 \text{ \AA}^3$ ,  $4.47 \text{ \AA}^3$  and  $2.21 \text{ \AA}^3$  (*i.e.*, 1.9 %, 6.7 % and 3.3 % larger, respectively).  $\beta\text{-Ag}_3\text{F}_4$  is an exception with small negative excess volume of  $-2.4 \text{ \AA}^3$  per FU (–2.5 %). These results suggest that various forms of the mixed valence  $\text{Ag}_2\text{F}_3$  are not packed as well as their binary counterparts. Hence they will not form at high pressure conditions (due to decomposition into the binary constituents). Rather, it is advisable to synthesize them at elevated temperature, which usually favors volume expansion. This surmise is analyzed in more detail in “Energetics of formation and impact of temperature”.

Phonons at  $\Gamma$ : indicator of dynamic stability

When predicting the possible occurrence of a novel phase or stoichiometry one should address its dynamic stability. It turns out that all phases calculated here do not exhibit imaginary phonon modes at the center of the first Brillouin zone ( $\Gamma$ ), which suggests their dynamic stability. The truncated (*i.e.*, calculated at  $\Gamma$  only) zero-point energy corrections to the formation energies (at  $T=0 \text{ K}$ , see next section) are ranging between  $-0.015 \text{ eV}$  and  $-0.038 \text{ eV}$ , and thus only slightly influence the formation energies (see next section).

Energetics of formation and impact of temperature

While considering the following formation reactions:



of mixed valence fluorides of silver with an increasing molar content of AgF (33%, 50%, 67%, respectively), we have calculated the energies of these reactions (Eq. 1–4).

It turns out that the energy of formation of  $\text{Ag}_3\text{F}_5$  (Eq. 1) is substantially positive, some 0.27 eV per FU. On the other hand, the energies of formation of  $\text{Ag}_2\text{F}_3$  (Eq. 2) are marginally negative for all three polymorphs (from  $-0.07 \text{ eV}$  to  $-0.03 \text{ eV}$  per FU) while that for  $\beta\text{-Ag}_3\text{F}_4$  (Eq. 3) is somewhat more negative ( $-0.17 \text{ eV}$ ). The formation energy of  $\text{Ag}_3\text{F}_4$  from  $\text{Ag}_2\text{F}_3$  and AgF (Eq. 4) is slightly negative, as well,  $-0.10 \text{ eV}$ , which suggests that  $\beta\text{-Ag}_3\text{F}_4$  should be the ultimate product of reaction between  $\text{AgF}_2$  and AgF as far as excess of AgF is used. The relatively small negative energy of formation of  $\text{Ag}_2\text{F}_3$  may be understood considering that formation of mixed-valence fluorides of silver is formally a Lewis acid–Lewis base reaction, for example  $\text{AgF}_2$  (acid)+AgF (base) $\rightarrow \text{Ag}^+[\text{AgF}_3^-]$ . Since AgF is a weak Lewis base as compared to MF ( $M=\text{K}, \text{Rb}, \text{Cs}$ ), formation of the  $\text{M}_{0.5}\text{AgF}_{2.5}$ ,  $\text{M}\text{AgF}_3$  and  $\text{M}_2\text{AgF}_4$  salts ( $M=\text{Ag}$ ) is not substantially favored. Taking a still different perspective one might say that formation of the mixed-valence systems is connected with the transformation of the lowest-energy 6-coordinated octahedral Ag(I) (in AgF) into either a trigonal bipyramidal, deformed tetrahedral, or 8-coordinated one, which, obviously, comes with an energy increase.

Interestingly, the smaller size of the Ag(I) cation as compared to K(I) results in a relative destabilization of  $\alpha\text{-Ag}_3\text{F}_4$  by over a quarter eV with respect to the ‘collapsed’  $\beta$ -form. Recollect, that for  $\text{K}_2\text{AgF}_4$  both polymorphs have virtually identical energy as calculated by LDA [42].

Small negative energies of formation for  $\text{Ag}_2\text{F}_3$  might be supplemented by a favourable entropy term at high temperatures, contributing to thermodynamic stability. An empirical relationship between  $S^\circ$  and the volume per FU,  $V_{\text{FU}}$ , for solid crystalline compounds, proposed by Mallouk and Bartlett [67, 68] was further extended to a wide variety of compounds by Jenkins and Glasser [69]. The correlation takes the form:

$$S^\circ [\text{J mol}^{-1} \text{K}^{-1}] = 1.757 \times V_{\text{FU}} (\text{\AA}^3) \quad (5)$$

The excess volumes of various polymorphs of  $\text{Ag}_2\text{F}_3$  as compared to binary substrates, range between 0 and  $4.5 \text{ \AA}^3$ ,

which translates to  $0\text{--}7.9\text{ J mol}^{-1}\text{ K}^{-1}$  in differential entropy of reaction,  $\Delta S^0$ . The corresponding maximum differential entropy term,  $[T \Delta S^0]$ , is  $-0.02\text{ eV}$  at 298 K and  $-0.07\text{ eV}$  at 900 K, thus it is comparable to or even exceeds the energy of formation of all polymorphs of  $\text{Ag}_2\text{F}_3$ , while contributing to their increased thermodynamic stability at elevated temperatures.

Concluding this section we would like to emphasize that it is worth pursuing synthesis of  $\text{Ag}_2\text{F}_3$  at elevated temperatures. Complete evaluation of thermodynamics of formation of mixed-valence fluorides of silver obviously requires precise resources-demanding calculations of full phonon dispersion and accurate reproduction of the lowest-energy phonon modes, and it is beyond the scope of the current study.

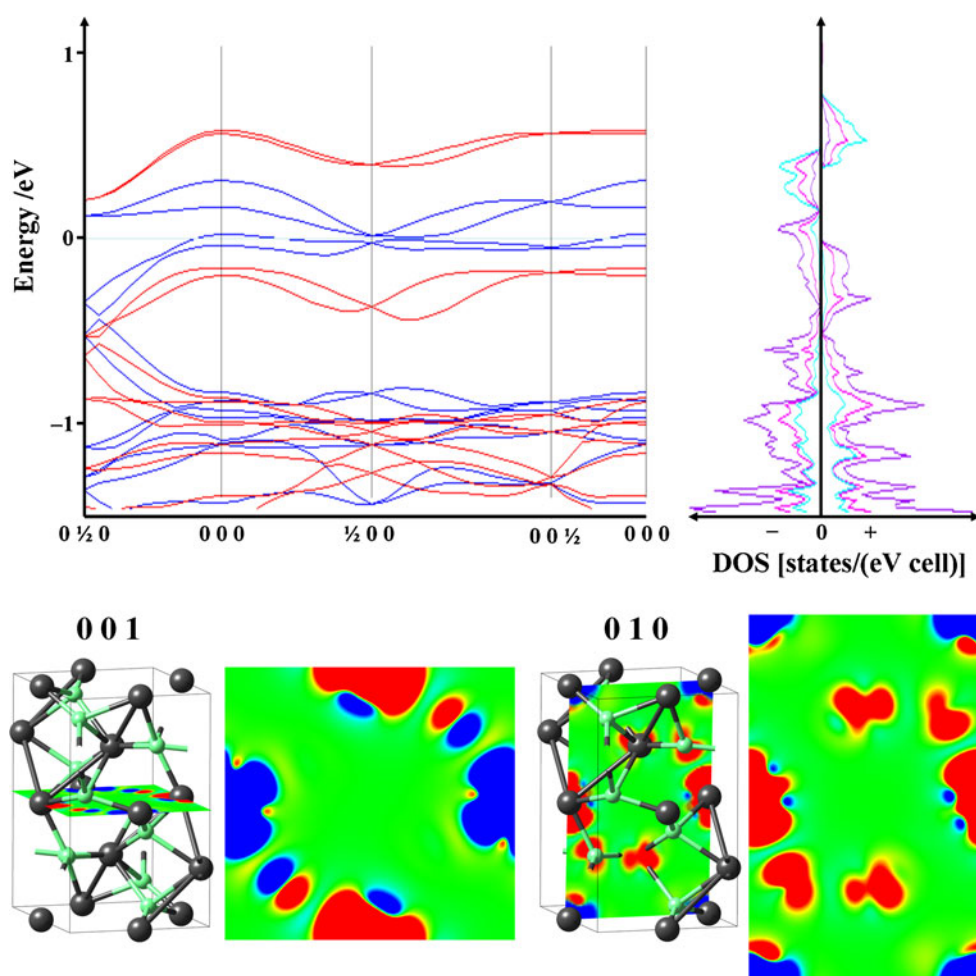
Mixed valence, electronic structure, band gap at the Fermi level and magnetism

$\text{Ag(II)}$  has a  $4d^9$  electronic configuration and it is paramagnetic. Electronic structure and magnetism of mixed-valence pseudobinary fluorides of silver, are there-

fore of interest. Will these compounds be metallic or insulating, show wide- or narrow-band gap, be ferro- or antiferromagnetic, similar to binary  $\text{AgF}_2$  or rather to ternary potassium fluoroargentates(II)? To answer these questions we have carried out calculations of the electronic band structures and electronic density of states for the most stable forms of  $\text{Ag}_2\text{F}_3$  and  $\text{Ag}_3\text{F}_4$  at the LSDA (not shown) and LSDA+U levels (Figs. 4 and 5).

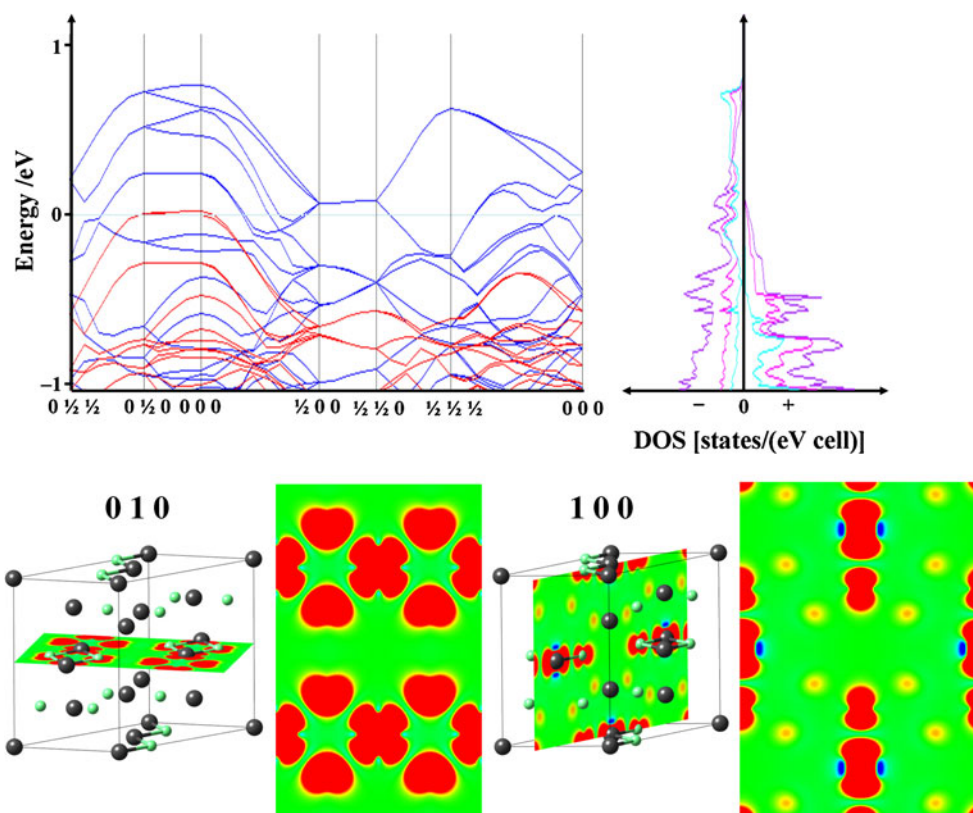
Inspection of the partial density of states shows that the electronic states predominated by 4d functions of  $\text{Ag(I)}$  cations are quite separated in energy from those of  $\text{Ag(II)}$  cations for the compounds studied. For example, the former are found in the  $(-1, 0)\text{ eV}$  energy window, while the latter in the  $(0, +1)\text{ eV}$  window for  $\alpha\text{-Ag(I)Ag(II)F}_3$ . This result is not surprising if we recollect that the coordination spheres of both types of cations were very different for all stoichiometries and polymorphs considered (*cf.* Sect. 3.1). In other words, the mixed valence fluorides of silver described in this work show genuine mixed- and not intermediate-valence. The vertical inter-valence charge transfer (IVCT) optical transitions are predicted to arise

**Fig. 4** The electronic band structure (majority spins – red, minority spins – blue) and electronic density of states for the most stable  $\alpha$  polymorph of  $\text{Ag(I)Ag(II)F}_3$ , with atomic contributions from F (rose), Ag(I) (violet) and Ag(II) (ocean blue) as calculated at the LSDA+U level. Projections of spin density (up to  $0.01\text{ e \AA}^3$ ) indicating magnetic superexchange pathways for facile magnetic superexchange, are also shown (blue and red stand for excess and depletion of  $\alpha$  density, respectively)





**Fig. 5** The electronic band structure (majority spins – red, minority spins – blue) and electronic density of states for the most stable  $\beta$  polymorph of  $\text{Ag(I)}_2\text{Ag(II)F}_4$ , with atomic contributions from F (rose), Ag(I) (violet) and Ag(II) (ocean blue) as calculated at the LSDA+U level. Projections of spin density (up to  $0.01 \text{ e } \text{\AA}^3$ ) indicating pathways for facile magnetic superexchange, are also shown (blue and red stand for excess and depletion of  $\alpha$  density, respectively)



between the highest occupied Ag(I) states and formally half-empty electron-deficient Ag(II) states; calculations (not taking into account the electron–hole attraction) locate the lowest energy IVCT transitions at less than 1 eV. These compounds should thus appear black to the eye and show metallic luster. All silver states are firmly hybridized with the 2p functions of F, like many others fluorides of silver [20].

It turns out that all structures with artificially enforced antiferromagnetic ordering of spins converge to metallic solutions at the LSDA level. This situation is quite typical for the late transition  $d^9$  systems such as  $\text{CuF}_2$  or  $\text{AgF}_2$  [70]. Inclusion of the on-site electron repulsion via a Hubbard U term (at the LSDA+U level) stabilizes magnetic solutions but does not open band gaps at the Fermi level (Figs. 4 and 5). Hence, the compounds studied may be labeled as magnetic metals.

All mixed valence fluorides of silver except for  $\alpha\text{-Ag}_3\text{F}_4$  show the coordination sphere of Ag(II) in the form of a more-or-less elongated octahedron. It is thus expected that magnetic coupling between the  $d(x^2-y^2)$  electrons (ferro- or antiferromagnetic in type) will depend only on a mutual orientation of the  $[\text{Ag(II)F}_4]$  plaquettes. If the Ag–F–Ag angle defining geometry of the fluoride bridge is close to  $180^\circ$ , antiferromagnetism is expected; if it is close to  $90^\circ$ , ferromagnetism should appear. The calculated Ag–F–Ag angle falls between these two values for all compounds studied here. For example, the intra-chain Ag–F–Ag angle

ranges from  $106.4^\circ$  for  $\beta\text{-Ag}_3\text{F}_4$  (double F bridge, ferromagnetism expected), via  $140.1^\circ$  for  $\alpha\text{-Ag}_2\text{F}_3$ , to  $140.6\text{--}142.9^\circ$  for  $\gamma\text{-Ag}_2\text{F}_3$  (single F bridge, antiferromagnetism more likely). The intra-sheet Ag–F–Ag angle ranges from  $122.6^\circ$  for  $\alpha\text{-Ag}_2\text{F}_3$  (ferromagnetism expected) via  $130.7^\circ$  for  $\gamma\text{-Ag}_2\text{F}_3$  and  $136.5^\circ$  for  $\beta\text{-Ag}_2\text{F}_3$ , to  $142.8^\circ$  for  $\alpha\text{-Ag}_3\text{F}_4$  (antiferromagnetic coupling possibly favored).

The LSDA+U calculations (Table 4) suggest that  $\beta\text{-Ag}_3\text{F}_4$  should indeed order ferromagnetically (in one dimension, along the propagation direction of the  $[\text{AgF}_{4/2}]$  chains) while  $\alpha\text{-Ag}_2\text{F}_3$  should show 3D magnetism with antiferromagnetic-type both intra- and inter-sheet coupling; due to different magnetic moments on crystallographically independent Ag(II) cations  $\alpha\text{-Ag}_2\text{F}_3$  should be described as ferrimagnet. The absolute values of the calculated magnetic moments on Ag(II) vary between  $0.34 \mu_B$  and  $0.44 \mu_B$  and they are smaller than those calculated for  $\text{AgF}_2$ ,  $\text{KAgF}_3$  and  $\beta\text{-K}_2\text{AgF}_4$  ( $0.51\text{--}0.56 \mu_B$ ). Those on bridging fluoride anions are in the  $0.08\text{--}0.11 \mu_B$  range, very close to the value calculated for  $\text{KAgF}_3$  ( $0.10 \mu_B$ ). As expected, Ag(I) cations carry rather little spin, with magnetic moments of  $0.14 \mu_B$  at most.

The approximate value of the magnetic superexchange constant, J, has been calculated from the following expression:

$$J \approx N_x \Delta E^{\text{AFM/FM}} \text{ (meV)} \quad (6)$$

**Table 4** The values of the intra-sheet or intra-chain (\*) magnetic superexchange constant ( $J$ /meV) and magnetic moments on Ag(II) and F centers, for five different mixed valence fluorides of silver as calculated

Compound	$\alpha$ -Ag <sub>2</sub> F <sub>3</sub>	$\beta$ -Ag <sub>3</sub> F <sub>4</sub>	AgF <sub>2</sub>	KAgF <sub>3</sub>	$\beta$ -K <sub>2</sub> AgF <sub>4</sub>
$J_{\text{LSDA+U}}$ /meV	-2*	+52**	-4.7***	ND**	ND**
$\mu(\text{Ag(II)})/\mu_{\text{B}}$	+0.38, -0.44	+0.34	$\pm 0.54$	$\pm 0.51$	$\pm 0.56$
$\mu(\text{Ag(I)})/\mu_{\text{B}}$	+0.03	+0.14	—	—	—
$\mu(\text{F}_{\text{bridge}})/\mu_{\text{B}}$	+0.09, -0.08	+0.11	0.00	$\pm 0.10$	+0.10
$\mu(\text{F}_{\text{terminal}})/\mu_{\text{B}}$	-0.01	+0.08	—	0.00, $\pm 0.10$	+0.10
Reference	This work	This work	[70]	[40]	[42]

\* 3D \*\* intra-chain (1D) \*\*\* intra-sheet (2D)

where  $N=2$  for 1D case,  $N=1$  for 2D case, and  $N=2/3$  for 3D case (Table 3). The value of  $J$  calculated for  $\alpha$ -Ag<sub>2</sub>F<sub>3</sub> is -2 meV, less than half of that predicted for AgF<sub>2</sub>; although the size of  $J$  is not impressive yet the type of magnetic ordering is of interest, rendering  $\alpha$ -Ag<sub>2</sub>F<sub>3</sub> the first candidate for a 3D fluoroargentate(II) antiferromagnet. On the other hand,  $J$  calculated for  $\beta$ -Ag<sub>3</sub>F<sub>4</sub> is as large as +52 meV, indicating strong ferromagnetic coupling via a [F<sub>2</sub>] bridge. Strong coupling must be due to the short Ag...Ag distance, and favorable value of the Ag-F-Ag (close to 90°). The absolute value of  $J$  is still smaller than the giant value of -298 meV predicted for the compressed 2D form of AgF<sub>2</sub> exhibiting flat [AgF<sub>2</sub>] sheets [71].

How might one attempt to synthesize Ag<sub>2</sub>F<sub>3</sub> and Ag<sub>3</sub>F<sub>4</sub>?

Conceivable existence of mixed-valence fluorides of silver (I/II) deduced from DFT calculations poses a question how these compounds might be synthesized in the laboratory.  $\beta$ -Ag<sub>3</sub>F<sub>4</sub> should be achieved quite easily, for example:

- Via prolonged exposure of AgF<sub>2</sub> to ultra-pure argon gas or at dynamic vacuum at temperatures slightly lower than its thermal decomposition temperature of 690 °C;
- Via photochemical decomposition of AgF<sub>2</sub>;
- Via electrochemical oxidation of saturated solutions of AgHF<sub>2</sub> in aHF on glassy carbon or platinum electrodes;
- Via high pressure synthesis, due to its more compact crystal structure than those for AgF and AgF<sub>2</sub>.

On the other hand, calculations suggest that Ag<sub>2</sub>F<sub>3</sub> is close to a thermodynamic equilibrium with a mixture of binary fluorides at 0 K and only slightly stabilized by the entropy term at elevated temperature conditions. It is thus advisable to use reagents capable of yielding exothermic reactions; the following preparative methods are suggested:

- Attempts of selective reduction of AgF<sub>2</sub> using C<sub>6</sub>F<sub>6</sub>, C<sub>10</sub>F<sub>8</sub>, C<sub>6</sub>Cl<sub>6</sub>, Cl<sub>2</sub> or similar poor reducing agents;

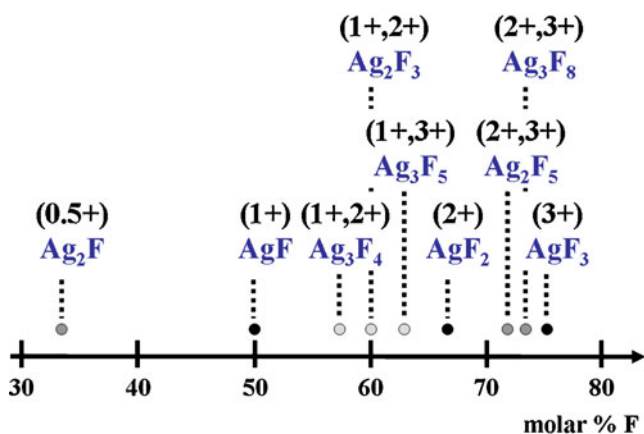
using LSDA+U method. Negative and positive sign of  $J$  stands for an antiferro- and ferromagnetic coupling, respectively. Values calculated for AgF<sub>2</sub> and KAgF<sub>3</sub> are shown for comparison. ND=not determined

- High-energy milling of AgF<sub>2</sub> and AgF in PTFE (Teflon®) mills; please note that local temperature at the intergrain boundary rises considerably when using this method;
- Alternative mechanochemical synthesis utilizing Ag(SbF<sub>6</sub>) and KAgF<sub>3</sub> or related reagents;
- Methathesis in anhydrous HF between M<sub>x</sub>(SbF<sub>6</sub>) (or related soluble salts) and excess of AgF (if formation of binary AgF<sub>2</sub> could be prevented (Mazej Z, Grochala W (2008) unpublished results)).

It is of interest if these theoretical predictions could be confirmed by experiments.

## Conclusions

Compounds containing silver at mixed valence (I/II) are immensely rare. The DFT calculations described in this work suggest conceivable existence of two novel mixed-valence Ag(I)/Ag(II) fluorides, Ag<sub>2</sub>F<sub>3</sub>≡Ag(I)Ag(II)F<sub>3</sub> and Ag<sub>3</sub>F<sub>4</sub>≡Ag(I)<sub>2</sub>Ag(II)F<sub>4</sub>, exhibiting crystal structures with



**Fig. 6** The known phases appearing in the Ag-F phase diagram together with hypothetical mixed-valence fluorides predicted in this work; molar % F and oxidation state(s) of Ag are shown

puckered  $[\text{AgF}_2]$  sheets and infinite  $[\text{AgF}_{4/2}]$  chains, respectively. The energies of formation from binary fluorides for the most stable polytypes of the mixed-valence compounds are predicted to be marginally negative, at the positive excess volume for  $\text{Ag}_2\text{F}_3$  and the negative one for  $\text{Ag}_3\text{F}_4$ .  $\text{Ag}_3\text{F}_4$  might thus be obtained directly from 2  $\text{AgF}$  and  $\text{AgF}_2$  but  $\text{Ag}_2\text{F}_3$  should be searched for either at high T conditions or as a product of various exothermic reactions. Both quasi-binary fluorides should exhibit mixed- and not intermediate valence, be strongly correlated metals, and order magnetically at low temperatures. The predicted intra-chain superexchange coupling constants,  $J$ , are  $-2$  and  $+52$  meV for the lowest energy  $\alpha$ - $\text{Ag}_2\text{F}_3$  and  $\beta$ - $\text{Ag}_3\text{F}_4$  polymorphs, respectively.  $\text{Ag}_3\text{F}_5$  is shown in fact to be a diamagnetic mixed valence  $\text{Ag(I)/Ag(III)}$  fluoride,  $\text{Ag(I)}_2\text{Ag(III)F}_5$ , thermodynamically unstable with respect to  $\text{AgF} / 2 \text{AgF}_2$  constituents.

A number of viable synthetic pathways are suggested which could help to confirm – or refute – these predictions in experiment. If synthesized, pseudo-binary  $\text{Ag}_2\text{F}_3$  and  $\text{Ag}_3\text{F}_4$  would enrich the spectrum of the known fluorides of silver:  $\text{Ag}_2\text{F}$ ,  $\text{AgF}$ ,  $\text{AgF}_2$ ,  $\text{AgF}_3$ ,  $\text{Ag}_2\text{F}_5$ , and  $\text{Ag}_3\text{F}_8$  (Fig. 6).

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## References

1.  $\text{Fe}_3\text{O}_4$  mentioned here is actually a more complex case, with Fe (III) cations at the A site of the spinel and both Fe(II) and Fe(III) cations at the B site
2. Robin MB, Day P (1967) *Adv inorg chem radiochem* 10:247–422
3. Marcus RA (1993) *Angew Chem Int Ed Engl* 32:1111–1121
4. Barbara PF, Meyer TJ, Ratner MA (1996) *J Phys Chem* 100: 13148–13168
5. Grochala W, Hoffman R (2000) *J Phys Chem A* 104:9740–9749 and references therein
6. Bednorz JG, Müller KA (1986) *Z Phys B Con Mat* 64:189–193
7. Williams A (1989) *J Phys Condens Mat* 1:2569–2574
8. Yoshida H, Muraoka Y, Sörgel T, Jansen M, Hiroi Z (2006) *Phys Rev B* 73:020408(R)-1 to -4
9. Schreyer M, Jansen M (2002) *Angew Chem Int Ed Engl* 41:643–646
10. Wang QM, Lee HK, Mak TCW (2002) *New J Chem* 26:513–515
11. Leung PC, Aubke F (1978) *Inorg Chem* 17:1765–1772
12. Michałowski T et al. (2010) 16th European Symposium on Fluorine Chemistry, Ljubljana Slovenia
13. Mazej Z (2010) Pacificchem – The International Chemical Congress of Pacific Basin Societies, Honolulu USA
14. Shen CP, Žemva B, Lucier GM, Graudejus O, Allman JA, Bartlett N (1999) *Inorg Chem* 38:4570–4577
15. McMillan JA (1960) *J Inorg Nucl Chem* 13:28–31
16. Robin MB, Andres K, Geballe TH, Kuebler NA, McWhan DB (1966) *Phys Rev Lett* 17:917–919
17. Standke B, Jansen M (2003) *Angew Chem Int Ed Engl* 25:77–78
18. Žemva B et al. (1991) *J Am Chem Soc* 113:4192–4198
19. Kraus M, Müller M, Fischer R, Schmidt R, Koller D, Müller BG (2000) *J Fluorine Chem* 101:165–171
20. Grochala W, Hoffmann R (2001) *Angew Chem Int Ed Engl* 40:2743–2781
21. Grochala W, Egdell RG, Edwards PP, Mazej Z, Žemva B (2003) *Chem Phys* 4:997–1001
22. Lucier GM, Münzenberg J, Casteel WJ, Bartlett N (1995) *Inorg Chem* 34:2692–2698
23. Grochala W, Edwards PP (2003) *Phys Status Solidi B* 240:R11–R14
24. Grochala W, Porch A, Edwards PP (2004) *Solid State Commun* 130:137–142
25. Grochala W (2005) *J Mol Model* 11:323–329
26. Grochala W (2009) *J Mater Chem* 19:6949–6968
27. Tokura Y, Tagaki H, Uchida S (1989) *Nature* 337:345–347
28. Grochala W, Feng J, Hoffmann R, Ashcroft NW (2006) *Angew Chem Int Ed Engl* 46:3620–3642
29. Blöchl PE (1994) *Phys Rev B* 50:17953–17979
30. Kresse G, Furthmüller J (1996) *Phys Rev B* 54:11169–11186
31. Kresse G, Furthmüller J (1996) *Comput Mater Sci* 6:15–50
32. Kresse G, Joubert D (1999) *Phys Rev B* 59:1758–1775
33. Vosko SH, Wilk L, Nusair M (1980) *Can J Phys* 58:1200–1211
34. Malinowski PJ, Derzsi M, Gaweł B, Łasocha W, Jagličić Z, Mazej Z, Grochala W (2010) *Angew Chem Int Edit* 49:1683–1686
35. Derzsi M, Dymkowski K, Grochala W (2010) *Inorg Chem* 49:2735–2742
36. Romiszewski J, Stolarczyk L, Grochala W (2007) *J Phys Condens Matter* 19:116206-1 to -13
37. Mazej Z et al. (2009) *Cryst Eng Comm* 11:1702–1710
38. Dudarev SL, Botton GA, Savrasov SY, Humphreys CJ, Sutton AP (1998) *Phys Rev B* 57:1505–1509
39. McLain SE et al. (2006) *Nat Mater* 5:561–566
40. Kurzydłowski D et al. (2010) 16th European Symposium on Fluorine Chemistry, Ljubljana Slovenia
41. Hidaka M, Inoue K, Yamada I, Walker PJ (1983) *Physica B+C* 121:343–350
42. Kurzydłowski D et al. (2010) *Eur J Inorg Chem* 19:2919–2925
43. Babel D (1965) *Z Anorg Allg Chem* 336:200–206
44. Buttner RH, Maslen EN, Spadaccini N (1990) *Acta Crystallogr B* 46:131–138
45. Hidaka M, Eguchi T, Yamada I (1998) *J Phys Soc Jpn* 67:2488–2494
46. Lindqvist O (1971) *Acta Chem Scand* 25:740–787
47. Kaiser V, Otto M, Binder F, Babel D (1990) *Z Anorg Allg Chem* 585:93–104
48. Tong J, Lee C, Whangbo MH, Kremer RK, Simon A Köhler J (2010) *Z Kristallogr* 12:680–684
49. Ghedira M, Anne M, Chenavas J, Marezio M, Sayetat F (1986) *J Phys C* 19:6489–6503
50. Müllerbuschbaum H, Wollschlager W (1975) *Z Anorg Allg Chem* 414:76–80
51. Bachmann B, Müller BG (1991) *Z Anorg Allg Chem* 597:9–18
52. Müller BG (1982) *Z Anorg Allg Chem* 491:245–252
53. Kaiser V, Babel D (1990) *Acta Crystallogr A* 46:367–368
54. Berastegui P, Hull S, Eriksson SG (2010) *J Solid State Chem* 183:373–378
55. Hoppe R, Homann R (1966) *Naturwiss* 53:501–501
56. Kurzydłowski D, Grochala W (2008) *Chem Commun* 1073–1075
57. Kurzydłowski D, Grochala W (2008) *Z Anorg Allg Chem* 634:1082–1086
58. Hoppe R (1957) *Z Anorg Allg Chem* 292:28–33

59. See Supplementary Information for Ref. [36] for DFT calculations
60. King G, Woodward PM (2010) *J Mater Chem* 20:5785–5796
61. Fischer P, Schwarzenbach D, Rietveld HM (1971) *J Phys Chem Solids* 32:543–550
62. Jesih A et al. (1990) *Z Anorg Allg Chem* 588:77–83
63. The  $P2_1/c$  cell is pseudo-orthorhombic ( $\beta=90.01^\circ$ ) and it may be symmetrized to Cmmm; this comes with energy bill of +0.02 eV per FU
64. Grochala W (2006) *Phys Statud Solidi B* 243:R81–R83
65. Mitrofanov VY, Nikiforov AE, Shashkin SY (1997) *Solid State Commun* 104:499–504
66. Feng J, Hennig RG, Ashcroft NW, Hoffmann R (2008) *Nature* 451:445–448
67. Bartlett N, Yeh S, Kourtakis K, Mallouk TE (1984) *J Fluorine Chem* 26:97–116
68. Shen CS, Hagiwara R, Mallouk TE, Bartlett N (1994) In: *Inorganic Fluorine Chemistry Toward the 21<sup>st</sup> Century*. American Chemical Society, Washington DC, p 26
69. Jenkins HDB, Glasser L (2003) *Inorg Chem* 42:8702–8708
70. Derzsi M, Leszczyński P, Grochala W (2010) unpublished data. Grochala W et al. (2010) 16<sup>th</sup> European Symposium on Fluorine Chemistry, Ljubljana Slovenia
71. Jaroń T, Grochala W (2008) *Phys Status Solidi R* 2:71–73